



UCD CASL

Complex & Adaptive Systems Laboratory

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Genetic Programming

COMP30290 Natural Computing
COMP41190 Natural Computing and Applications



Genetic Programming

Automatic Programming

- ▶ Assemblers;
- ▶ Compilers 2GL;
- ▶ Automatic Parallelisation.

Arthur Samuel, 1959:

*“Tell the computer what to do,
not how to do it.”*





Genetic Programming

John Koza's AP attributes. . .

- ▶ Start with **high-level problem description** that results in a solution in the form of a computer program;
- ▶ Automatically determine the program's **size and architecture**;
- ▶ Automatically organise a group of **instructions** so that they may be **re-used** by a program;
- ▶ **Problem-independence**;
- ▶ **Scalability** to larger versions of the same problem;
- ▶ Capability of producing **human competitive results**;
- ▶ Evolutionary Automatic Programming / Genetic Programming.



Genetic Programming

Individual is OR **represents/encodes** a program

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>

int main(int argc, char* argv){
    float x=0.0, y=0.0, z=0.0;
    x=atof(argv[1]);
    y=atof(argv[2]);
    z=atof(argv[3]);
    x = 2.0*sin(y) + 4.0*sin(x);
    z = (x*x) + exp(z);
    printf("The answer is: z=%f\n",z);
    return(0);
}
```

```
#include <stdio.h>
#include <stdlib.h>
#include <math.h>

void turnLeft(float degrees);
void turnRight(float degrees);
void moveForward(float distance);

int main(int argc, char* argv){
    turnLeft(90);
    if(sensorValue(0) > 1000)
        moveForward(10);
    else
        turnRight(90);
    return(0);
}
```



Representation

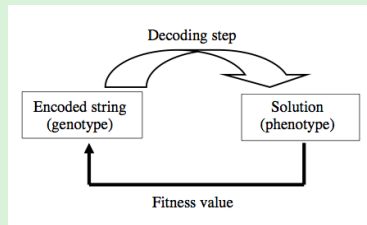
Recall GAs

- ▶ Binary string;
- ▶ Fixed-length chromosomes;
- ▶ Problem specific encoding.
- ▶ But how to encode a program?...

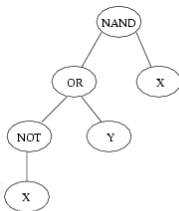
Representation

The Road to GP

- ▶ Historical Perspective on Representation
 - ▶ Friedberg (1958/1959);
 - ▶ Cramer (1985);
 - ▶ Koza (1989).
- ▶ Distinguishing features:
 - ▶ Variable-length;
 - ▶ GP operates on solution directly.



Representation

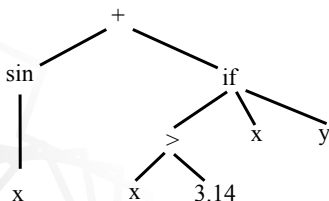


(NAND (OR (NOT X) Y) X)

GP trees

- ▶ Koza (1992) popularised Lisp S-expressions;
- ▶ Expressions (trees) generated from:
 - ▶ *Function Set*: boolean, arithmetic, loops, user-defined functions...
 - ▶ *Terminal Set*: inputs, constants, variables...

Representation



Different types of functions/terminals

- ▶ Conditionals;
- ▶ (if (> x 3.14) x y)
- ▶ IF 'condition' THEN 'return X' ELSE 'return y'



Representation

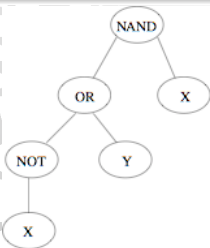
Features

- ▶ Sufficiency:
 - ▶ Function + Terminal sets: powerful enough to represent a solution.
- ▶ Parsimony:
 - ▶ Smaller Function + Terminal sets are better.
- ▶ Closure:
 - ▶ Each function should gracefully handle all values it ever receives;
 - ▶ (/ 5 0) ?!?

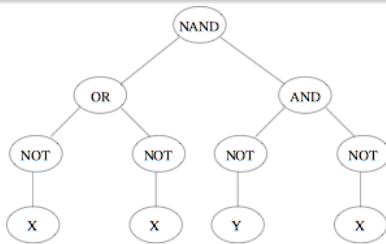
Initialisation

Tree Creation

- ▶ Max Depth - Maximum Program Size;
- ▶ **Grow** and **Full** initialisation;
- ▶ Desire structural diversity:
 - ▶ **Ramped half-and-half.**



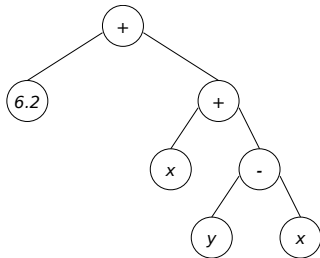
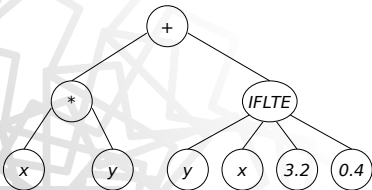
Grow – Depth 4



Full – Depth 4



Initialisation



Genetic Operators

Operators

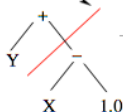
- ▶ Crossover;
- ▶ Mutation;
- ▶ Reproduction.

| | | | | | | | |
|-----------|-------------|--|-----------|---|-------------|------------------|-----------|
| P1 | 0 2 1 0 4 4 | | 0 1 1 2 1 | → | 0 2 1 0 4 4 | <u>0 0 4 3 3</u> | C1 |
| P2 | 3 3 1 5 1 0 | | 0 0 4 3 3 | | 3 3 1 5 1 0 | <u>0 1 1 2 1</u> | C2 |

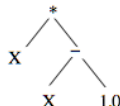
Crossover
Point



P1



P2



C1



C2



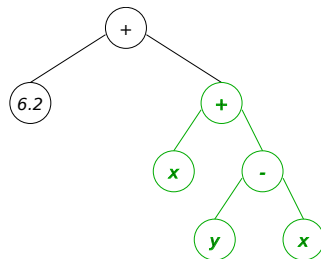
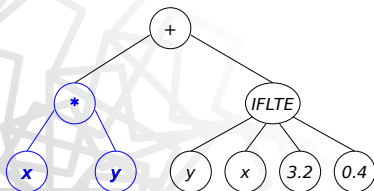
Genetic Operators

Crossover

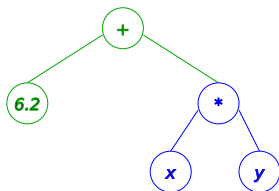
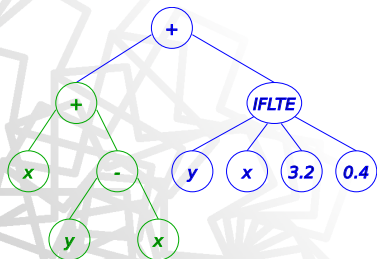
1. Select two parents;
2. For first parent, randomly pick node from 1 to n ;
3. Independently pick node from 1 to n for second parent;
4. Swap sub-trees.



Crossover



Crossover



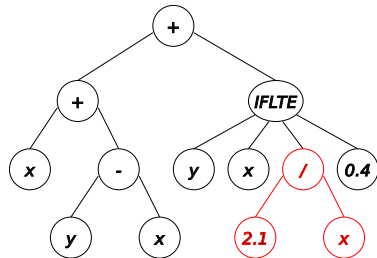
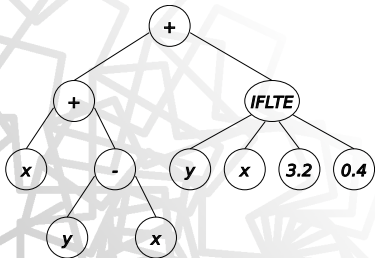


Genetic Operators

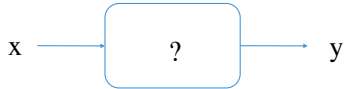
Mutation

1. Randomly pick node from 1 to n ;
2. Delete subtree at selected node;
3. Grow new subtree (as per initialisation).

Mutation



Parametrisation



Problem Definition

- ▶ Find function that gives output (y) for specific input (x);
- ▶ $y = f(x)$;
- ▶ E.g. $f(x) = x^2 + x$

Preparatory Steps

- ▶ Define function and terminal set;
- ▶ Define fitness measure;
- ▶ Define evolutionary parameters:
 - ▶ Max-depth, popsize, xover prob., mut. prob., reproduction prob., selection & replacement strategies, termination criteria.



Fitness Measure

Fitness Function

- ▶ Problem specific;
- ▶ Design to give graded and continuous feedback for selection:
 - ▶ Continuous fitness function;
 - ▶ Standardised fitness;
 - ▶ Normalised fitness.

Fitness Measure

$$f(x) = x^2 + x$$

Fitness Function

| case # | Input | Output |
|--------|-------|--------|
| 1 | 1 | 2 |
| 2 | 2 | 6 |
| 3 | 4 | 20 |
| 4 | 7 | 56 |
| 5 | 9 | 90 |

- ▶ Simple discrete form: $f_p = \sum_{i=1}^n (p_i == o_i)$
- ▶ Simple continuous form: $f_p = \sum_{i=1}^n |p_i - o_i|$
- ▶ Mean Squared Error: $f_p = \frac{\sum_{i=1}^n (p_i - o_i)^2}{n}$

Fitness Measure

Fitness Function

| case # | Input | Output (o_i) | Prediction (p_i) | Error | Squared Error |
|--------|-------|------------------|----------------------|-------|----------------|
| 1 | 1 | 2 | 1 | 1 | 2 |
| 2 | 2 | 6 | 4 | 2 | 4 |
| 3 | 4 | 20 | 16 | 4 | 16 |
| 4 | 7 | 56 | 49 | 7 | 49 |
| 5 | 9 | 90 | 81 | 9 | 81 |
| | | | | 23 | 151 / 5 = 30.2 |

- ▶ Different fitness functions = different fitness landscapes;
- ▶ Co-evolution:
 - ▶ No explicit fitness value;
 - ▶ Fitness relative to other individuals.
- ▶ Multi-objective fitness functions.



Next Classes

- ▶ Notes on Selection (available online).
- ▶ Lecture Tuesday 24th September 15h - 16h;
 - ▶ GP applications/variations;
 - ▶ Structure of 2-page proposal.